

Building on Foundations – Virtual

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Welcome!

Building on Foundations









Opening Outcomes



Participants will...

Consider how the mathematical storyline provides opportunities to foster curiosity, make connections, and deepen understanding.

Purposefully use the embedded resources to plan for sharing math authority with students.

Reflect on past year(s) of teaching CPM curriculum and consider ways to enhance your collaborative classroom.

Develop an action plan to support your ongoing professional learning.

Agenda Building on Foundations





Opening & Icebreaker
 Mathematical Storyline
 Sharing Math Authority
 Creating Collaborative Classrooms
 Closure

Welcome Working Agreements

Click on your name and set your status to thumbs up if you are ready to begin.

Be willing to take **risks**. Have a **visionary** mindset. Stay **engaged**. Explore and reflect on your **beliefs**. Give **grace** to others and yourself.

Change takes time, effort, and support!

Opening Research Connections CPM Implementation Progress Tool





The three pillars represent researched best practice in math education around which the CPM program is designed.

Collaborative Learning

Research says students learn ideas more deeply when they discuss ideas with classmates.

Problem-Based Learning

Research says students learn ideas more usefully for other arenas when they learn by attacking problems.

Mixed, Spaced Practice

Research says students learn ideas more permanently when they are required to engage and re-engage with those ideas for months or even years.



Agenda Building on Foundations





Opening & Icebreaker
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Icebreaker The Joy of Teaching





PERSONALIZE WITH PICTURES TO REPRESENT YOUR TEACHING STORIES.

Icebreaker The Joy of Teaching

Why/how did you become a teacher?





Collaborative Classrooms Visibly Random Teams



Let's practice collaboration with new teams!



https://pickerwheel.com/tools/random-team-generator/

Agenda Building on Foundations Building on Assessment



Mixed, Spaced Practice

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Outcome: Consider how the mathematical storyline provides opportunities to foster curiosity, make connections, and deepen understanding.

Mathematical Storyline Does the sequence of events matter?







Mathematical Storyline







(The Mathematics Teacher, Dietiker, November 2016) Used with permission from the publisher for CPM Learning Events. May not be reproduced or redistributed by others without permission. Mathematical Storyline Mathematical Story Defined



"Seeing how mathematics unfolds, connecting a beginning to an ending, so that somebody who is experiencing it can kind of sense a storyline and predict where it's going."



Episode 13: Where Joel and Misty Make a new friend with Dr. Leslie Dietiker and talk about Mathematical Storylines

Mathematical Storyline

Experience a Mathematical Story:

CC1 Lesson 7.2.2





Method 1: Using diagrams





To divide any number by a fraction using a diagram, create a model of the situation using rectangles, a linear model, or some visual representation of it. Then break that model into the fractional parts named.

For example, to divide $\frac{7}{8} \div \frac{1}{2}$, you can draw the diagram at right to visualize how many $\frac{1}{2}$ -sized pieces fit into $\frac{7}{8}$. The diagram shows that one $\frac{1}{2}$ fits one time, with $\frac{3}{8}$ of a whole left. Since $\frac{3}{8}$ is $\frac{3}{4}$ of $\frac{1}{2}$, you can see that $1\frac{3}{4}$ $\frac{1}{2}$ -sized pieces fit into $\frac{7}{8}$, so $\frac{7}{8} \div \frac{1}{2} = 1\frac{3}{4}$.

Alternately, you could think of $\frac{7}{8}$ as the quantity that you have and $\frac{1}{2}$ as the size of the group that you want, such as having $\frac{7}{8}$ ounces of chocolate and needing $\frac{1}{2}$ ounce for each cake recipe. How many cakes could you make? In this case, the diagram at right might be useful. The diagram shows $\frac{7}{8}$ being divided into groups of $\frac{1}{2}$. The leftover $\frac{3}{8}$ ounces creates another $\frac{3}{4}$ of a group, so again, $\frac{7}{8} \div \frac{1}{2} = 1\frac{3}{4}$.

Method 2: Using Common Denominators

To divide a number by a fraction using common denominators, express both numbers as fractions with the same denominator. Then divide the first numerator by the second. An example is shown at right.

$\frac{1}{2} \quad \frac{3}{4} \text{ of } \frac{1}{2}$



 $\begin{array}{l} \frac{2}{5} \div \frac{3}{10} = \frac{4}{10} \div \frac{3}{10} \\ = 4 \div 3 \\ = \frac{4}{3} = 1\frac{1}{3} \end{array}$

7-53. Calculate each of the following products. <u>Homework Help </u>

a.
$$\frac{1}{8} \cdot \frac{8}{1}$$
 b. $\frac{3}{4} \cdot \frac{4}{3}$ c. $\frac{2}{3} \cdot \frac{3}{2}$ d. 7.

e. What do the products in parts (a) through (d) have in common?

 $\frac{1}{7}$

Mathematical Storyline Experience a Mathematical Story



7.2.3 How can I divide?

Division with Fractions and Decimals

This lesson will bring you more division strategies! You will continue your work with dividing fractions to include a new strategy for dividing by fractions. You will also extend your knowledge to division of decimals.

Mathematical Storyline Experience a Mathematical Story





Your Task:

Examine the problems and consider the mathematical storyline.

Change the order of the problems.

- 1. How does the sequence foster curiosity for students?
- 2. How does changing the sequence affect the story?



Find the missing number in each puzzle.					
<i>i</i> . 6 · = 1					
<i>ii</i> . 4 · = 1					
<i>iii.</i> ⅔ · = 1					

Malik was working on the division problem $5 \div \frac{3}{4}$.

Copy the expression and simplify it.

Cheryl used the problem ½ ÷ ¾.

Copy and complete Cheryl's calculation.

Mathematical Storyline Experience a Mathematical Story: CC1 Lesson 7.2.3





Math Goal: Divide fractions using the Giant One strategy.

Success criteria for the task:

- + Teams know there is a storyline within the lesson.
- + Teams understand the intentional design.
- + Teams analyze how leveraging this design supports the mathematics progression.



Mathematical Storyline

Debrief the Storyline





How does the authors' chosen sequence provide opportunities for surprise and intrigue?

What are the mathematical characters, settings, and actions? Where/What was the "aha" of this lesson?

Mathematical Storyline Definition

"Enacting a sequence so that it offers dramatic conflict can also offer students a memorable experience and, since it increases student attention, lead to more learning by students (Egan 1989)."

Mathematics Teacher, November 2016



MATHEMATICAL STORYLINE				
	0	Introduction		
	2	Discussion Post (Mathematical Storyline)		
	\bigcirc	More Math for More People - Dr. Leslie Dietiker and Mathematical Storylines		
	\bigcirc	Mathematical Storyline Scenarios		
	Ç	Scenario A: Productive Struggle		
		Restricted Not available unless: You belong to Group A		
	Ç	Scenario B: Structure and Organization		
		Restricted Not available unless any of: You belong to Group B The activity Scenario A: Productive Struggle is marked complete		
	\bigcirc	Lesson Planning		
	0	Action Plan (Mixed, Space Practice)		
	\bigcirc	Activity 1 Completed		

Agenda Building on Foundations Building on Discourse



Problem-Based Learning

Research says students learn ideas more usefully for other arenas when they learn by attacking problems. Opening & Icebreaker
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Outcome: Purposefully use the embedded resources to plan for sharing math authority with students.

Opening



CPM's Equity Principles

The goal of teaching is to help all students transition from dependent to independent learners.

Relationships are of vital importance. Student uniqueness is an asset, not a deficit.

Reflection is a crucial part of growth.

Sharing Math Authority Research Connection







SECTION TWO: Features of desired student learning when the pillars are in place.

Collaborative Learning	Problem-Based Learning	Mixed, Spaced Practice
Students read and make sense of problems together.	Student thinking at varied depths of conceptual understanding are openly shared and valued.	Students work through lessons at an appropriate pace.
Students are able to listen to the ideas of others and communicate their own ideas both in teams and during whole class discussions.	Students demonstrate and value both conceptual and procedural knowledge.	Students understand that mastery takes time, effort, and support.
Students listen carefully to the thinking of others and respond with clarifying questions or extensions of their own.	Students look for, compare, and connect multiple models and solution strategies.	Students are aware of learning targets and periodically self-assess their progress towards those targets.
Students engage in productive mathematical discourse, justifying answers, creating viable arguments, and critiquing the reasoning of others.	Students recognize that incorrect work can be a stepping stone to learning and are willing to share and investigate their thinking.	Students solidify learning as they work on Review & Preview problem sets daily as intended.

Review these evidence statements.

2. Set your status with how you feel as you reflect on your own classroom.



Sharing Math Authority Self Reflection





Two Stars and a Wish

What is going well?

What is a challenge?

Two Stars and a Wish				
Star 🔶				
Star 🔶				
Wish 💫				

Sharing Math Authority

Resources Concept Map



Chapter Closure



Classroom/Team Expectations

Sharing Math Authority

Resources Concept Map







Facilitator: Universal Access, Pocket Questions

Resource Manager: Skill Builders, Math Notes

Recorder/Reporter: Teambuilders/Icebreakers, Homework Help

Task Manager: Team Roles, Checkpoints



Explore your assigned resources. Consider the following questions. (4 min)

- + How do these resources support sharing math authority?
- + What connections do you see to the Mathematical Teaching Practices?

Consider a STTS that supports sharing the math authority?

Sharing Math Authority Debrief



Embedded CPM Resources

Suggested Lesson Plan Study Team & Teaching Strategies Pocket Questions Mathcast Universal Access Lesson Plan Structure: (Launch–Explore –Closure) Learning Logs

Team Roles Classroom/Team Expectations Chapter Opening Chapter Closure Homework Help Math Notes Checkpoint Problems Skillbuilders

Agenda Building on Foundations Building on Equity



Collaborative Learning

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Outcome: Reflect on past year(s) of teaching CPM curriculum and consider ways to enhance your collaborative classroom.

Collaborative Classrooms Debrief



Reflect on your team's collaboration.



What does collaboration <u>**not</u>** look like?</u>



What does collaboration look like?

Create a Collaboration Rubric Idea from Building Thinking Classrooms

Collaborative Classrooms

On-Demand Module





Agenda Building on Foundations





Opening & Icebreaker
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Outcome: Develop an action plan to support your ongoing professional learning.

Opening	J
Outcomes	



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Closure CPM Implementation Progress Tool

Building on...



SECTION ONE: The pillars that represent necessary first steps in any implementation.

Collaborative Learning

Students and teachers are aware of the purpose for and value of working in teams, and are familiar with team norms and roles.

Problem-Based Learning

Students and teachers share math authority as they value and engage in productive struggle. Teachers guide without taking over the thinking.

Mixed, Spaced Practice

Both individual lessons and chapters are followed, using suggested pacing. Review & Preview problems are assigned and valued as an essential part of learning.

Assessment





Closure

- + Parking Lot
- + Attendance

XXXXX

- + Continuing Education Credit
- + Homework:
 - On-Demand Module
 - Building on Foundations





Insert QR Code Here





